

## **Unit-III (Functional dependencies and Normalization, Relational Data Model and Relational Algebra)**

### **Important questions**

#### **Section A :(2 Marks)**

##### **1.What is Functional Dependency?**

Functional dependency (FD) is set of constraints between two attributes in a relation. Functional dependency says that if two tuples have same values for attributes A<sub>1</sub>, A<sub>2</sub>,..., A<sub>n</sub> then those two tuples must have same values for attributes B<sub>1</sub>, B<sub>2</sub>, ..., B<sub>n</sub>. Functional dependency is represented by arrow sign ( $\rightarrow$ ), that is X $\rightarrow$ Y, where X functionally determines Y. The left hand side attributes determines the values of attributes at right hand side.

##### **2.What are the applications of Relational Algebra?**

The main application of relational algebra is providing a theoretical foundation for relational databases, particularly query languages for such databases.

##### **3.Define Normalization. What is the use of Normalization?**

Normalization is the process of organizing the attributes and tables of a relational database to minimize data redundancy.

Normalization is the process of reorganizing data in a database so that it meets two basic requirements:

- a) There is no redundancy of data (all data is stored in only one place).
- b) Data dependencies are logical (all related data items are stored together).

##### **4. What are the types of Normalization?**

First normal form

Second normal form

Third normal form

Boyce-Codd Normal form

#### **Section-B: (5 Marks and 10 Marks)**

##### **1.Explain Functional Dependency in Detail.**

Functional dependency (FD) is set of constraints between two attributes in a relation. Functional dependency says that if two tuples have same values for attributes A<sub>1</sub>, A<sub>2</sub>,..., A<sub>n</sub> then those two tuples must have same values for attributes B<sub>1</sub>, B<sub>2</sub>, ..., B<sub>n</sub>. Functional dependency is

represented by arrow sign ( $\rightarrow$ ), that is  $X \rightarrow Y$ , where X functionally determines Y. The left hand side attributes determines the values of attributes at right hand side.

#### Armstrong's Axioms

William W. Armstrong established a set of rules which can be used to Infer the functional dependencies in a relational database:

Reflexivity rule:  $A \rightarrow A$  is true, if B is subset of A. Augmentation rule: If  $A \rightarrow B$  is true, then  $AC \rightarrow BC$  is also true. Transitivity rule: If  $A \rightarrow B$  and  $B \rightarrow C$ , then  $A \rightarrow C$  is implied.

## 2.Explain various types of Normal forms with examples.

### FIRST NORMAL FORM (1NF)

First normal form: A table is in the first normal form if it contains no repeating columns.

Consider the below table, in this example it shows several employees working on several projects. In this company the same employee can work on different projects and at a different hourly rate. Convert this table into 1NF.



Project Code	Project Title	Project Manager	Project Budget	Employee No	Employee Name	Department No	Department Name	Hourly Rate
PC10	MIS	Nisarga	24500	S10001	ARUN	L004	IT	22
PC10	MIS	Nisarga	24500	S10030	LOKESH	L023	Pionix	18
PC10	MIS	Nisarga	24500	S21010	PAVANI	L004	IT	21
PC45	LIS	Eenchara	17400	S10010	BABU	L004	IT	21
PC45	LIS	Eenchara	17400	S10001	ARUN	L004	IT	18
PC45	LIS	Eenchara	17400	S31002	TULASI	L028	Database	25
PC45	LIS	Eenchara	17400	S13210	WILLIAM	L008	Systems	17
PC64	HMS	Prakruthi	12250	S31002	TULASI	L028	Database	23
PC64	HMS	Prakruthi	12250	S21010	PAVANI	L004	IT	17
PC64	HMS	Prakruthi	12250	S10034	BALU	L009	HR	16

**UNF:UnNormalized Table**

#### STEPS:

Transform a table of unnormalised data into first normal form (1NF). The process is as follows:

Identify repeating attributes.  
 Remove these repeating attributes to a new table togetherwith a copy of the key from the UNF table. After removing the duplicate data the repeating attributes are easily identified. In the previous table the Employee No, Employee Name, Department No, Department Name and Hourly Rate attributes are repeating. These are the repeating attributes and have been to a new table together with a copy of the original key (ie:Project Code).

A key of Project Code and Employee No has been defined for this new table. This combination is unique for each row in the table.

- 

### **1NF Tables: Repeating Attributes Removed**

Project Code	Project Title	Project Manager	Project Budget
PC10	MIS	Nisarga	24500
PC45	LIS	Eenchara	17400
PC64	HMS	Prakruthi	12250

Project Code	Employee No	Employee Name	Department No	Department Name	Hourly Rate
PC10	S10001	ARUN	L004	IT	22
PC10	S10030	LOKESH	L023	Pionix	18
PC10	S21010	PAVANI	L004	IT	21
PC45	S10010	BABU	L004	IT	21
PC45	S10001	ARUN	L004	IT	18
PC45	S31002	TULASI	L028	Database	25
PC45	S13210	WILLIAM	L008	Systems	17
PC64	S31002	TULASI	L028	Database	23
PC64	S21010	PAVANI	L004	IT	17
PC64	S10034	BALU	L009	HR	16

### **SECOND NORMAL FORM (2NF)**

Second normal form: A table is in the second normal form if it is in the first normal form and contains only columns that are dependent on the whole (primary) key.

STEPS:

Transform 1NF data into second normal form (2NF). Remove any -key attributes (partial Dependencies) that only depend on part of the table key to a new table. Ignore tables with a simple key or with no non- key attributes.

The first table went straight to 2NF as it has a simple key (Project Code).

Employee name, Department No and Department Name are dependent upon Employee No only. Therefore, they were moved to a new table with Employee No being the key.

However, Hourly Rate is dependent upon both Project Code and Employee No as an employee may have a different hourly rate depending upon which project they are working on. Therefore it remained in the original table.

## 2NF Tables: Partial Key Dependencies Removed

<b>Project Code</b>	<b>Project Title</b>	<b>Project Manager</b>	<b>Project Budget</b>
PC10	MIS	Nisarga	24500
PC45	LIS	Eenchara	17400
PC64	HMS	Prakruthi	12250

<b>Project Code</b>	<b>Employee No</b>	<b>Hourly Rate</b>
PC10	S10001	22
PC10	S10030	18
PC10	S21010	21
PC45	S10010	21
PC45	S10001	18
PC45	S31002	25
PC45	S13210	17
PC64	S31002	23
PC64	S21010	17
PC64	S10034	16

<b>Employee No</b>	<b>Employee Name</b>	<b>Department No</b>	<b>Department Name</b>
S10001	ARUN	L004	IT
S10030	LOKESH	L023	Pionix
S21010	PAVANI	L004	IT
S10010	BABU	L004	IT
S31002	TULASI	L028	Database
S13210	WILLIAM	L008	Systems
S10034	BALU	L009	HR

### THIRD

### NORMAL

### FORM

### (3NF)

Third normal form: A table is in the third normal form if it is in the second normal form and all the non-key columns are dependent only on the primary key. If the value of a non-key column is dependent on the value of another non-key column we have a situation known as transitive dependency. This can be resolved by removing the columns dependent on non-key items to another table.

#### STEPS:

Data in second normal form (2NF) into third normal form (3NF). Remove to a new table any non-key attributes that are more dependent on other non-key attributes than the table key.

The project team table went straight from 2NF to 3NF as it only has one non-key attribute. Department Name is more dependent upon Department No than Employee No and therefore was moved to a new table. Department No is the key in this new table and a foreign key in the Employee table.

## 3NF Tables: Non-Key Dependencies Removed

<b>Project Code</b>	<b>Project Title</b>	<b>Project Manager</b>	<b>Project Budget</b>
PC10	MIS	Nisarga	24500
PC45	LIS	Eenchara	17400
PC64	HMS	Prakruthi	12250

<b>Project Code</b>	<b>Employee No</b>	<b>Hourly Rate</b>
PC10	S10001	22
PC10	S10030	18
PC10	S21010	21
PC45	S10010	21
PC45	S10001	18
PC45	S31002	25
PC45	S13210	17
PC64	S31002	23
PC64	S21010	17
PC64	S10034	16

<b>Employee No</b>	<b>Employee Name</b>	<b>Department No</b>
S10001	ARUN	L004
S10030	LOKESH	L023
S21010	PAVANI	L004
S10010	BABU	L004
S31002	TULASI	L028
S13210	WILLIAM	L008
S10034	BALU	L009

<b>Department No</b>	<b>Department Name</b>
L004	IT
L023	Pionix
L028	Database
L008	Systems
L009	HR

### Boyce-Codd Normal Form(BCNF)

A table is in Boyce-Codd normal form (BCNF) if and only if it is in 3NF and every determinant is a candidate key. Anomalies can occur in relations in 3NF if there is a composite key in which part of that key has a determinant which is not itself a candidate key.

This can be expressed as R(A,B,C), C--->A where:

- o The relation R contains attributes A, B and C
- o A and B form a candidate key.
- o C is the determinant for A (A is functionally dependent on C).
- o C is not part of any key.

Anomalies can also occur where a relation contains several candidate keys where:

- o The keys contain more than one attribute (they are composite keys).
- o An attribute is common to more than one key. Example to understand BCNF:-

Consider the following non-BCNF table:

### Nearest Shops

Person	Shop Type	Nearest Shop
Ashwini	Optician	Eagle Eye
Ashwini	Hairdresser	Snippets
Chaya	Bookshop	GK Books
Namita	Bakery	Dlight
Namita	Hairdresser	Sweet Stall
Namita	Optician	Eagle Eye

The candidate key of the table are: {Person, Shop Type}

{Person, Nearest Shop}

The table does not adhere to BCNF because of the dependency

Nearest Shop  $\rightarrow$  Shop Type, in which the determining attribute (Nearest shop) is neither a candidate key nor a superset of a candidate key.

After Normalization.

Shop Near Person		Shop	
Person	Shop	Shop	Shop Type
Ashwini	Eagle Eye	Eagle Eye	Optician
Ashwini	Snippets	Snippets	Hairdresser
Chaya	GK Books	GK Books	Bookshop
Namita	Dlight	Dlight	Bakery
Namita	Sweet Stall	Sweet Stall	Hairdresser
Namita	Eagle Eye	Eagle Eye	Optician

Candidate keys are {Person, Shop} and {Shop}, respectively.

### 3.Explain various types of operations in Relational Algebra.

#### Relational Algebra

➤ Basic operations:

- ✓ *Projection ( $\Pi$ )* Selects a subset of columns from relation.
- ✓ *Selection ( $\sigma$ )* Selects a subset of rows from relation.

- ✓ *Cross-product* ( $\times$ ) Allows us to combine two relations.
- ✓ *Set-difference* (-) Tuples in reln. 1, but not in reln. 2.
- ✓ *Union* (U) Tuples in reln. 1 and in reln. 2.
- ✓ *Rename( p)* Use new name for the Tables or fields.

➤ Additional operations:

- ✓ *Intersection* ( $\cap$ ), *join()*.

## PROJECT ( $\pi$ )

The PROJECT operation is used to select a subset of the attributes of a relation by specifying the names of the required attributes

Consider the Student\_table:

A) For example, to get a name from Student\_Table.  $\pi_{\text{Name}}(\text{Student\_Table})$

<b>Regno</b>	<b>Name</b>	<b>Gender</b>	<b>Course</b>
101	Varsha G Kalyan	F	BCA
102	Mohith G Kalyan	M	BBM
103	Nisarga	F	Bcom
104	Rama	M	BCA

<b>Name</b>
Varsha G Kalyan
Mohith G Kalyan
Nisarga
Rama

## SELECT( $\sigma$ )

The SELECT operation is used to choose a subset of the tuples from a relation that satisfies a selection condition. the SELECT operation can be consider to be a filter that keeps only those tuples that satisfy a qualifying condition.

A) For example, to list the regno> 102 from Student\_Table.  $\sigma_{\text{Regno}>102}(\text{Student\_table})$

<b>Regno</b>	<b>Name</b>
101	Varsha G Kalyan
102	Mohith G Kalyan
103	Nisarga
104	Rama

<b>Regno</b>	<b>Name</b>	<b>Gender</b>	<b>Course</b>
103	Nisarga	F	Bcom
104	Rama	M	BCA

B) For example, to list all the Students belong to BCA course.  $\sigma_{\text{Course}=\text{"BCA"}}$ (Student\_table)

<b>Regno</b>	<b>Name</b>	<b>Gender</b>	<b>Course</b>
101	Varsha G Kalyan	F	BCA
104	Rama	M	BCA

## UNION Operator

List of customers who are either borrower or depositor at bank  $\pi_{\text{Cust-name}}(\text{Borrower}) \cup \pi_{\text{Cust-name}}(\text{Depositor})$

BORROWER

<b>Cust-name</b>	<b>Loan_no</b>
Ram	L-13
Shyam	L-30
Suleman	L-42

DEPOSITOR

<b>Cust-name</b>	<b>Acc-No</b>
Suleman	A-100
Radeshyam	A-300
Ram	A-401

<b>Cust-name</b>
Ram
Shyam
Suleman
Radeshyam

## INTERSECTION Operator

Customers who are both borrowers and depositors  $\pi_{\text{Cust-name}}(\text{Borrower}) \cap \pi_{\text{Cust-name}}(\text{Depositor})$

## Set Difference

Cust-name
Ram
Suleman

Customers who are borrowers but not depositors  $\pi_{\text{Cust-name}}(\text{Borrower}) - \pi_{\text{Cust-name}}(\text{Depositor})$

Cust-name
Suleman

## Cartesian-Product or Cross-Product ( $S1 \times R1$ )

Each row of S1 is paired with each row of R1.

- Result schema has one field per field of S1 and R1, with fieldnames 'inherited' if possible.
- Consider the borrower and loan tables as follows:

BORROWER		Loan	
Cust-name	Loan_no	Loan_no	Loan_Amt
Ram	L-13	L-13	10000
Shyam	L-30	L-30	20000
Suleman	L-42	L-42	40000

Borrower	Cust-name	Borrower	Loan_no	Loan	Loan_No	Loan	Loan_Amt
Ram		L-13		L-13		10000	
Ram		L-13		L-30		20000	
Ram		L-13		L-42		40000	
Shyam		L-30		L-13		10000	
Shyam		L-30		L-30		20000	
Shyam		L-30		L-42		40000	
Suleman		L-42		L-13		10000	
Suleman		L-42		L-30		20000	
Suleman		L-42		L-42		40000	

## JOIN

Join is combination of Cartesian product followed by selection process. Join operation pairs two tuples from different relations if and only if the given join condition is satisfied.

Following section describe briefly about join types:

## Natural Join ( $\bowtie$ )

Natural Join can only be performed if there is at least one common attribute exists between relation. Those attributes must have same name and domain.

Natural join acts on those matching attributes where the values of attributes in both relation is same.

Courses		
CID	Course	Dept
CS01	Database	CS
ME01	Mechanics	ME
EE01	Electronics	EE

HoD	
Dept	Head
CS	Alex
ME	Maya
EE	Mira

Courses $\bowtie$ HoD			
Dept	CID	Course	Head
CS	CS01	Database	Alex
ME	ME01	Mechanics	Maya
EE	EE01	Electronics	Mira

## Theta ( $\theta$ ) join

Theta joins combines tuples from different relations provided they satisfy the theta condition.

Notation:  $R1 \bowtie_\theta R2$

$R1$  and  $R2$  are relations with their attributes  $(A_1, A_2, \dots, A_n)$  and  $(B_1, B_2, \dots, B_n)$  such that no attribute matches that is  $R1 \cap R2 = \emptyset$ . Here  $\theta$  is condition in form of set of conditions  $C$ .

Theta join can use all kinds of comparison operators ( $=, <, >, \leq, \geq, \neq$ ).

Student\_Detail = STUDENT  $\bowtie$  Student.Std = Subject.Class SUBJECT

## Equi-Join

When Theta join uses only equality comparison operator it is said to be Equi-Join. The above example corresponds to equi-join.

Student		
SID	Name	Std
101	Alex	10
102	Maria	11

Subjects	
Class	Subject
10	Math
10	English
11	Music
11	Sports

Student_detail				
SID	Name	Std	Class	Subject
101	Alex	10	10	Math
101	Alex	10	10	English
102	Maria	11	11	Music
102	Maria	11	11	Sports

#### 4.Explain relational model constraints in detail.

Integrity Constraints over Relations

---

An integrity constraint (IC) is a condition that is specified on a database schema, and restricts the data that can be stored in an instance of the database.

Integrity constraints are specified and enforced at different times:

1. When the DBA or end user defines a database schema, he or she specifies the ICs that must hold on any instance of this database.
2. When a database application is run, the DBMS checks for violations and disallows changes to the data that violate the specified ICs.

## Key Constraints

It is a set of one or more columns whose combined values are unique among all occurrences in a given table. A key is the relational means of specifying uniqueness. Some different types of keys are:

Primary key is an attribute or a set of attributes of a relation which posses the properties of uniqueness and irreducibility (No subset should be unique). For example: Register Number in Student table is primary key, Passenger Number in passenger table is primary key, Passport number in Booking table is a primary key and the combination of passenger number and Passport Number in Reservation table is a primary key ie composite primary key.

Foreign key is the attributes of a table, which refers to the primary key of some another table. Foreign key permit only those values, which appears in the primary key of the table to which it refers or may be null (Unknown value).

For example: Register number of Result table refers to the Register number of Student table, which is the primary key of Student table, so we can say that Register number of Result table is the foreign key.

Student Table

<u>Registernumber</u>	Name	Course

Result Table

Registernumber	Course	Sem	Result